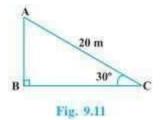


EXERCISE 9.1

PAGE NO: 203

1. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole, if the angle made by the rope with the ground level is  $30^{\circ}$ . (see fig. 9.11)



### **Solution:**

Length of the rope is 20 m and angle made by the rope with the ground level is 30°.

**Given:** AC = 20 m and angle  $C = 30^{\circ}$ 

**To Find**: Height of the pole Let AB be the vertical pole

In right  $\triangle$ ABC, using sine formula sin

 $30^{\circ} = AB/AC$ 

Using value of sin 30 degrees is ½, we have

1/2 = AB/20

AB = 20/2

AB = 10

Therefore, the height of the pole is 10 m.

2. A tree breaks due to storm and the broken part bends so that the top of the tree touches the ground making an angle  $30^{\circ}$  with it. The distance between the foot of the tree to the point where the top touches the ground is 8 m. Find the height of the tree.

### **Solution:**

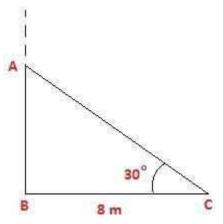
Using given instructions, draw a figure. Let AC be the broken part of the tree. Angle  $C = 30^{\circ}$  BC

= 8 m

To Find: Height of the tree, which is AB



### 



From figure: Total height of the tree is the sum of AB and AC i.e. AB+AC

In right  $\triangle ABC$ ,

Using Cosine and tangent angles, cos

$$30^{\circ} = BC/AC$$

We know that,  $\cos 30^{\circ} = \sqrt{3/2}$ 

$$\sqrt{3/2} = 8/AC$$

$$AC = 16/\sqrt{3} ...(1)$$

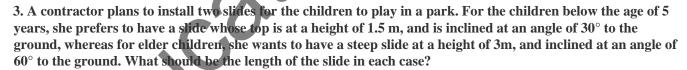
Also, 
$$\tan 30^{\circ} =$$

AB/BC

$$1/\sqrt{3} = AB/8$$

$$AB = 8/\sqrt{3}$$
 ....(2)

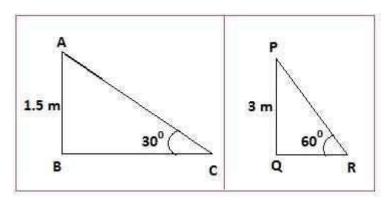
Therefore, total height of the tree = AB + AC =  $16\sqrt{3} + 8/\sqrt{3} = 24/\sqrt{3} = 8\sqrt{3}$  m.



#### **Solution**:

As per contractor's plan.

Ages	Height of Slide	Inclined Angle
Below 5 years	1.5 m	30 degrees
Above 5 years	3 m	60 degrees



Let, ABC is the slide inclined at  $30^{\circ}$  with length AC and PQR is the slide inclined at  $60^{\circ}$ 

with length PR.

To Find: AC and PR

In right  $\triangle ABC$ , sin

 $30^{\circ} = AB/AC$ 

1/2 = 1.5/AC

AC = 3 Also,

In right  $\triangle PQR$ , sin

 $60^{\circ} = PQ/PR$ 

 $\Rightarrow \sqrt{3/2} = 3/PR$ 

 $\Rightarrow$  PR =  $2\sqrt{3}$ 

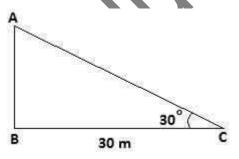
Hence, length of the slide for below 5 = 3 m and

Length of the slide for elders children = 2\days m

4. The angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower, is  $30^{\circ}$ . Find the height of the tower.

### **Solution:**

Let AB be the height of the tower and C is the point elevation which is 30 m away from the foot of the tower.



To Find: AB (height of the tower)

In right ABC



# Chapter 9 \_ Some Applications of Trigonometry

 $\tan 30^{\circ} = AB/BC$ 

 $1/\sqrt{3} = AB/30$ 

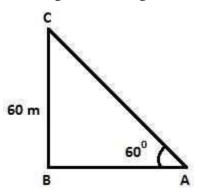
 $\Rightarrow$  AB =  $10\sqrt{3}$ 

Thus, the height of the tower is  $10\sqrt{3}$  m.

5. A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is  $60^{\circ}$ . Find the length of the string, assuming that there is no slack in the string.

### **Solution:**

Draw a figure, based on given instruction,



Let BC = Height of the kite from the ground, <math>BC = 60 m

AC = Inclined length of the string from the ground and A

is the point where string of the kite is tied.

To Find: Length of the string from the ground i.e. the value of AC

From the above figure,  $\sin 60^{\circ} = BC/AC$ 

 $\Rightarrow \sqrt{3/2} = 60/AC$ 

 $\Rightarrow$  AC =  $40\sqrt{3}$  m

Thus, the length of the string from the ground is  $40\sqrt{3}$  m.

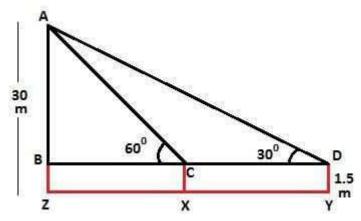
6. A 1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyes to the top of the building increases from  $30^{\circ}$  to  $60^{\circ}$  as he walks towards the building. Find the distance he walked towards the building.

### **Solution:**

Let the boy initially stand at point Y with inclination  $30^{\circ}$  and then he approaches the building to the point X with inclination  $60^{\circ}$ .



# **Some Applications of Trigonometry**



To Find: The distance boy walked towards the building i.e. XY

From figure, XY

= CD.

Height of the building = AZ = 30 m.

$$AB = AZ - BZ = 30 - 1.5 = 28.5$$

Measure of AB is 28.5 m

In right ΔABD, tan

$$30^{\circ} = AB/BD$$

$$1/\sqrt{3} = 28.5/BD$$

BD =  $28.5\sqrt{3}$  m Again,

In right ΔABC, tan

$$60^{\circ} = AB/BC$$

$$\sqrt{3} = 28.5/BC$$

BC = 
$$28.5/\sqrt{3} = 28.5\sqrt{3}/3$$

Therefore, the length of BC is 28.5 \( \frac{3}{3} \) m.

$$XY = CD = BD - BC = (28.5\sqrt{3} - 28.5\sqrt{3}/3) = 28.5\sqrt{3}(1-1/3) = 28.5\sqrt{3} \times 2/3 = 57/\sqrt{3} = 19\sqrt{3} \text{ m}.$$

Thus, the distance boy walked towards the building is  $19\sqrt{3}$  m.

7. From a point on the ground, the angles of elevation of the bottom and the top of a transmission tower fixed at the top of a 20 m high building are  $45^{\circ}$  and  $60^{\circ}$  respectively. Find the height of the tower.

### **Solution:**

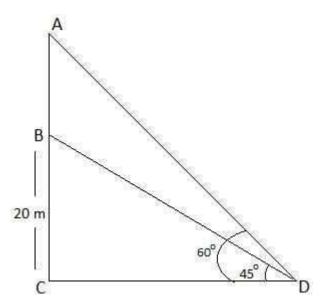
Let BC be the 20 m high building.

D is the point on the ground from where the elevation is taken.

Height of transmission tower = AB = AC - BC



# Chapter 9 \_ Some Applications of Trigonometry



To Find: AB, Height of the tower

From figure, In right  $\Delta BCD$ , tan

 $45^{\circ} = BC/CD$ 

1 = 20/CD

CD = 20 Again,

In right ΔACD, tan

 $60^{\circ} = AC/CD$ 

 $\sqrt{3} = AC/20$ 

 $AC = 20\sqrt{3}$ 

Now,  $AB = AC - BC = (20\sqrt{3}-20) = 20(\sqrt{3}-1)$  Height

of transmission tower =  $20(\sqrt{3})$  m.

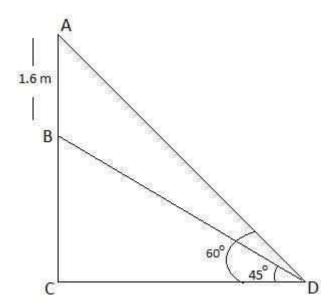
8. A statue, 1.6 m tall, stands on the top of a pedestal. From a point on the ground, the angle of elevation of the top of the statue is  $60^{\circ}$  and from the same point the angle of elevation of the top of the pedestal is  $45^{\circ}$ . Find the height of the pedestal.

### Solution:

Let AB be the height of statue.

D is the point on the ground from where the elevation is taken.

To Find: Height of pedestal = BC = AC-AB



From figure,

In right triangle BCD,

$$\tan 45^{\circ} = BC/CD 1 =$$

BC/CD

$$BC = CD \dots (1)$$

Again,

In right ΔACD, tan

$$60^{\circ} = AC/CD$$

$$\sqrt{3} = (AB+BC)/CD$$

$$\sqrt{3}\text{CD} = 1.6 + \text{BC}$$

 $\sqrt{3}BC = 1.6 + BC$  (using equation (1)

$$\sqrt{3}BC - BC = 1.6$$

$$BC(\sqrt{3}-1) = 1.6$$

BC = 
$$[(1.6)(\sqrt{3}+1)]/[(\sqrt{3}-1)(\sqrt{3}+1)]$$

BC = 
$$[1.6(\sqrt{3}+1)]/(2)$$
 m

BC = 
$$0.8(\sqrt{3+1})$$

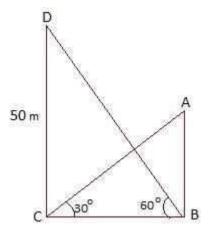
Thus, the height of the pedestal is  $0.8(\sqrt{3}+1)$  m.

9. The angle of elevation of the top of a building from the foot of the tower is  $30^{\circ}$  and the angle of elevation of the top of the tower from the foot of the building is  $60^{\circ}$ . If the tower is 50 m high, find the height of the building.



### **Solution:**

Let CD be the height of the tower. AB be the height of the building. BC be the distance between the foot of the building and the tower. Elevation is 30 degree and 60 degree from the tower and the building respectively.



In right  $\triangle BCD$ , tan

 $60^{\circ} = CD/BC$ 

 $\sqrt{3} = 50/BC$ 

BC =  $50/\sqrt{3}$  ...(1) Again,

In right ΔABC, tan

 $30^{\circ} = AB/BC$ 

 $\Rightarrow 1/\sqrt{3} = AB/BC$ 

Use result obtained in equation (1)

AB = 50/3

Thus, the height of the building is 50/3 m.

10. Two poles of equal heights are standing opposite each other on either side of the road, which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are  $60^{\circ}$  and  $30^{\circ}$ , respectively. Find the height of the poles and the distances of the point from the poles.

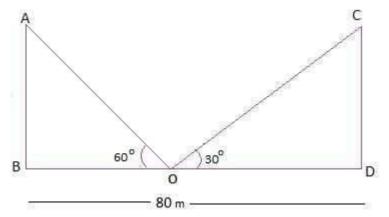
### **Solution:**

Let AB and CD be the poles of equal height.

O is the point between them from where the height of elevation taken. BD is the distance between the poles.



# Chapter 9 \_ Some Applications of Trigonometry



As per above figure, AB = CD,

$$OB + OD = 80 \text{ m}$$

Now,

In right ΔCDO, tan

$$30^{\circ} = CD/OD$$

$$1/\sqrt{3} = CD/OD$$

$$CD = OD/\sqrt{3} \dots (1)$$
 Again,

In right ΔABO, tan

$$60^{\circ} = AB/OB$$

$$\sqrt{3} = AB/(80-OD)$$

$$AB = \sqrt{3(80-OD)}$$

$$AB = CD$$
 (Given)

$$\sqrt{3}(80\text{-OD}) = \text{OD}/\sqrt{3}$$
 (Using equation (1)

$$3(80-OD) = OD$$

$$240 - 3 \text{ OD} = \text{OD}$$

$$4 \text{ OD} = 240$$

$$OD = 60$$

Putting the value of OD in equation (1)

$$CD = OD/\sqrt{3}$$

$$CD = 60/\sqrt{3}$$

$$CD = 20\sqrt{3} \text{ m}$$

Also,

$$OB + OD = 80 \text{ m}$$

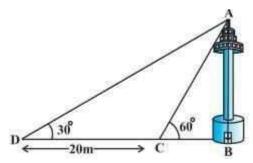


# Chapter 9 \_ Some Applications of Trigonometry

 $\Rightarrow$  OB = (80-60) m = 20 m

Thus, the height of the poles are  $20\sqrt{3}$  m and distance from the point of elevation are 20 m and 60 m respectively.

11. A TV tower stands vertically on a bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is  $60^{\circ}$ . From another point 20 m away from this point on the line joing this point to the foot of the tower, the angle of elevation of the top of the tower is  $30^{\circ}$  (see Fig. 9.12). Find the height of the tower and the width of the canal.



Solution: Given, AB is the height of the tower. DC

= 20 m (given)

As per given diagram, In right ΔABD, tan

 $30^{\circ} = AB/BD$ 

 $1/\sqrt{3} = AB/(20+BC)$ 

 $AB = (20+BC)/\sqrt{3}$  ... (i) Again,

In right  $\triangle$ ABC, tan

 $60^{\circ} = AB/BC$ 

 $\sqrt{3} = AB/BC$ 

 $AB = \sqrt{3} BC \dots (ii)$ 

From equation (i) and (ii)

 $\sqrt{3} BC = (20+BC)/\sqrt{3}$ 

3 BC = 20 + BC

2 BC = 20

BC = 10

Putting the value of BC in equation (ii)

 $AB = 10\sqrt{3}$ 

This implies, the height of the tower is  $10\sqrt{3}$  m and the width of the canal is 10 m.

12. From the top of a 7 m high building, the angle of elevation of the top of a cable tower is  $60^{\circ}$  and the angle of depression of its foot is  $45^{\circ}$ . Determine the height of the tower.



### 

### **Solution**:

Let AB be the building of height 7 m and EC be the height of the tower.

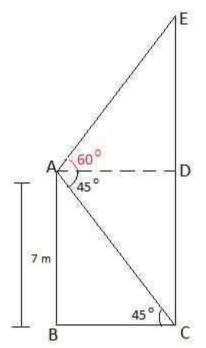
A is the point from where elevation of tower is 60° and the angle of depression of its foot is 45°.

$$EC = DE + CD$$

Also, 
$$CD = AB = 7 \text{ m.}$$
 and  $BC = AD$ 

To Find: EC = Height of the tower

Design a figure based on given instructions:



In right ΔABC, tan

$$45^{\circ} = AB/BC$$

1 = 7/BC

$$BC = 7$$

Since 
$$BC = AD$$

Again, from right triangle ADE, tan

$$60^{\circ} = DE/AD$$

$$\sqrt{3} = DE/7$$

$$\Rightarrow$$
 DE =  $7\sqrt{3}$  m

Now: 
$$EC = DE + CD$$

$$=(7\sqrt{3}+7)=7(\sqrt{3}+1)$$



Therefore, height of the tower is  $7(\sqrt{3}+1)$  m. Answer!

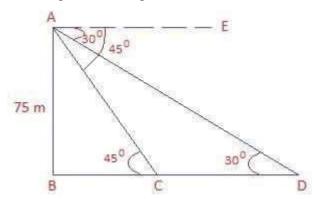
13. As observed from the top of a 75 m high lighthouse from the sea-level, the angles of depression of two ships are  $30^{\circ}$  and  $45^{\circ}$ . If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships.

### **Solution:**

Let AB be the lighthouse of height 75 m. Let C and D be the positions of the ships.

 $30^{\circ}$  and  $45^{\circ}$  are the angles of depression from the lighthouse.

Draw a figure based on given instructions:



To Find: CD = distance between two ships

Step 1: From right triangle ABC, tan 45°

= AB/BC

1 = 75/BC

BC = 75 m

Step 2: Form right triangle ABD, tan

 $30^{\circ} = AB/BD$ 

 $1/\sqrt{3} = 75/BD$ 

 $BD = 75\sqrt{3}$ 

Step 3: To find measure of CD, use results obtained in step 1 and step 2.

$$CD = BD - BC = (75\sqrt{3} - 75) = 75(\sqrt{3}-1)$$

The distance between the two ships is  $75(\sqrt{3}-1)$  m. Answer!

14. A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is  $60^{\circ}$ . After some time, the angle of elevation reduces to  $30^{\circ}$  (see Fig. 9.13). Find the distance travelled by the balloon during the interval.



# **Some Applications of Trigonometry**

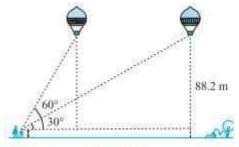
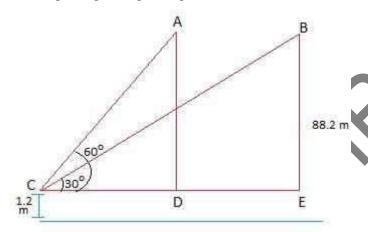


Fig. 9.13

### **Solution:**

Let the initial position of the balloon be A and final position be B. Height of balloon above the girl height = 88.2 m - 1.2 m = 87 m. To Find: Distance travelled by the balloon = DE = CE – CD Let us redesign the given figure as per our convenient



Step 1: In right  $\Delta BEC$ , tan

 $30^{\circ} = BE/CE$ 

 $1/\sqrt{3} = 87/CE$ 

 $CE = 87\sqrt{3} \text{ Step}$ 

2:

In right  $\triangle ADC$ , tan

 $60^{\circ} = AD/CD$ 

 $\sqrt{3} = 87/\text{CD}$ 

 $CD = 87/\sqrt{3} = 29\sqrt{3} \text{ Step}$ 

3:



DE = CE – CD =  $(87\sqrt{3} - 29\sqrt{3}) = 29\sqrt{3}(3 - 1) = 58\sqrt{3}$  Distance

travelled by the balloon =  $58\sqrt{3}$  m.

15. A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of  $30^{\circ}$ , which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be  $60^{\circ}$ . Find the time taken by the car to reach the foot of the tower from this point.

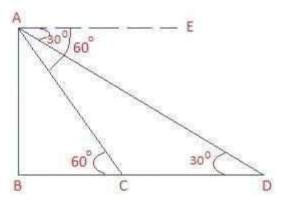
### **Solution:**

Let AB be the tower.

D is the initial and C is the final position of the car respectively.

Since the man is standing at the top of the tower so, Angles of depression are measured from

BC is the distance from the foot of the tower to the car.



Step 1: In right  $\triangle$ ABC, tan

 $60^{\circ} = AB/BC$ 

 $\sqrt{3} = AB/BC$ 

 $BC = AB/\sqrt{3}$ 

 $AB = \sqrt{3} BC$ 

Step 2:

In right ΔABD, tan

 $30^{\circ} = AB/BD$ 

 $1/\sqrt{3} = AB/BD$ 

 $AB = BD/\sqrt{3}$ 

Step 3: Form step 1 and Step 2, we have

 $\sqrt{3}$  BC = BD/ $\sqrt{3}$  (Since LHS are same, so RHS are also same)

3 BC = BD



### 

3 BC = BC + CD

2BC = CD or BC

= CD/2

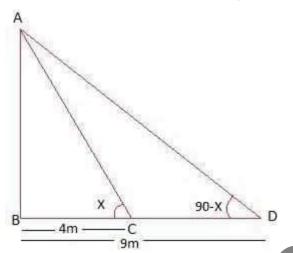
Here, distance of BC is half of CD. Thus, the time taken is also half.

Time taken by car to travel distance CD = 6 sec. Time taken by car to travel BC = 6/2 = 3 sec.

16. The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower and in the same straight line with it are complementary. Prove that the height of the tower is 6 m.

### **Solution:**

Let AB be the tower. C and D be the two points with distance 4 m and 9 m from the base respectively. As per question,



In right  $\triangle ABC$ ,

tan x = AB/BC tan

x = AB/4

 $AB = 4 \tan x \dots (i)$ 

Again, from right ΔABD,

 $tan (90^{\circ}-x) = AB/BD co$ 

x = AB/9

 $AB = 9 \cot x$  . (ii

Multiplying equation (i) and (ii)

 $AB^2 = 9 \cot x \times 4 \tan x$ 

 $\Rightarrow$  AB<sup>2</sup> = 36 (because cot x = 1/tan x

 $\Rightarrow$  AB =  $\pm$  6

Since height cannot be negative, therefore, the height of the tower is 6 m.



Hence Proved.